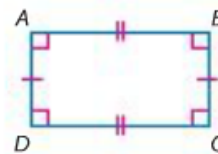


1 Properties of Rectangles A **rectangle** is a parallelogram with four right angles. By definition, a rectangle has the following properties.

- All four angles are right angles.
- Opposite sides are parallel and congruent.
- Opposite angles are congruent.
- Consecutive angles are supplementary.
- Diagonals bisect each other.



Rectangle ABCD

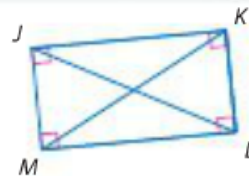
In addition, the diagonals of a rectangle are congruent.

Theorem 6.13 Diagonals of a Rectangle

If a parallelogram is a rectangle, then its diagonals are congruent.

Abbreviation If a \square is a rectangle, *diag. are \cong* .

Example If $\square JKLM$ is a rectangle, then $\overline{JL} \cong \overline{MK}$.



Rectangle has ALL the properties of a parallelogram (7) Plus 4 right angles and \cong diagonals (2). \rightarrow 9 total.

All rectangles are parallelograms, but not all parallelograms are rectangles.

2 Prove that Parallelograms are Rectangles The converse of Theorem 6.13 is also true.

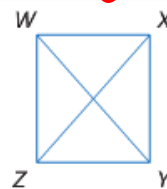
Converse: Switches order of hypothesis / conclusion.

Theorem 6.14 Diagonals of a Rectangle *TEST for Rectangle.*

If the diagonals of a parallelogram are congruent, then the parallelogram is a rectangle.

Abbreviation *If diag. of a \square are \cong , then \square is a rectangle.*

Example If $\overline{WY} \cong \overline{XZ}$ in $\square WXYZ$, then $\square WXYZ$ is a rectangle.

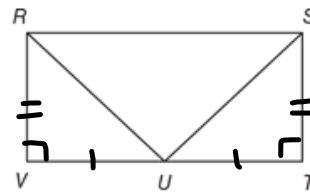


Example 1: Write a two-column proof.

PROOF: Write a two-column proof.

Given: $RSTV$ is a rectangle and U is the midpoint of \overline{VT} .

Prove: $\triangle RUV \cong \triangle SUT$



STATEMENTS	REASONS
1. $RSTV$ is a rectangle and U is the midpoint of \overline{VT} .	1. Given
2. $\overline{UV} \cong \overline{UT}$	2. Def. of midpoint.
3. $\overline{RV} \cong \overline{ST}$	3. Opp. sides of \square are \cong .
4. $\angle V$ and $\angle T$ are Right \angle s	4. Rectangle has 4 right \angle s.
5. $\angle V \cong \angle T$	5. All right \angle s are \cong .
6. $\triangle RUV \cong \triangle SUT$	6. SAS.

ALGEBRA Quadrilateral $ABCD$ is a rectangle.



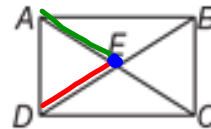
diagonals of rectangle are \cong .

2. If $AC = 2x + 13$ and $DB = 4x - 1$, find DB .

$$\begin{aligned}
 AC &= DB \\
 2x + 13 &= 4x - 1 \\
 -2x + 13 & \quad | \quad -2x + 1 \\
 \hline
 14 &= 2x \\
 \frac{14}{2} &= \frac{2x}{2} \\
 7 &= x
 \end{aligned}$$

$$\begin{aligned}
 DB &= 4(7) - 1 \\
 &= 28 - 1 \\
 DB &= 27
 \end{aligned}$$

ALGEBRA Quadrilateral $ABCD$ is a rectangle.



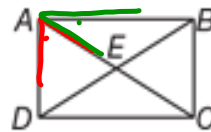
3. If $DE = 6x - 7$ and $AE = 4x + 9$, find DB .

$$\begin{aligned}
 DE &= AE \\
 6x - 7 &= 4x + 9 \\
 -4x + 7 & \quad | \quad -4x + 7 \\
 \hline
 2x &= 16 \\
 \frac{2x}{2} &= \frac{16}{2} \\
 x &= 8
 \end{aligned}$$

$$\begin{aligned}
 DB &= 2DE \\
 DB &= 2(6 \cdot 8 - 7) \\
 DB &= 2(48 - 7) \\
 DB &= 2(41) \\
 \boxed{DB} &= \boxed{82}
 \end{aligned}$$

- ① Diagonals of rectangles are \cong
- ② Diagonals bisect each other
 $E = \text{midpoint}$

ALGEBRA Quadrilateral $ABCD$ is a rectangle.



4. If $m\angle DAC = 2x + 4$ and $m\angle BAC = 3x + 1$, find $m\angle BAC$.

$$m\angle DAC + m\angle BAC = 90$$

$$2x + 4 + 3x + 1 = 90$$

$$5x + 5 = 90$$

$$\downarrow -5 \quad | \quad -5$$

$$5x = 85$$

$$\frac{5x}{5} = \frac{85}{5}$$

$$x = 17$$

Rect. has 4 right angles

$$m\angle BAC = 3(17) + 1$$

$$51 + 1$$

$$\textcircled{52}$$

ALGEBRA Quadrilateral $ABCD$ is a rectangle.

5. If $m\angle ABD = 7x - 31$ and $m\angle CDB = 4x + 5$, find $m\angle ABD$.

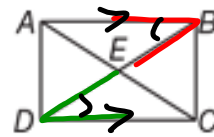
$$m\angle ABD = m\angle CDB$$

$$7x - 31 = 4x + 5$$

$$\begin{array}{r} -4x + 31 \quad | \quad -4x + 31 \\ \hline \end{array}$$

$$\frac{3x}{3} = \frac{36}{3}$$

$$x = 12$$



alternate interior angles are \cong

$$m\angle ABD = 7(12) - 31$$

$$84 - 31$$

$$\textcircled{53}$$